

Code No: 155EV

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech III Year I Semester Examinations, January/February - 2023

DESIGN AND ANALYSIS OF ALGORITHMS

(Computer Science and Information Technology)

Time: 3 Hours

Max. Marks: 75

Note: i) Question paper consists of Part A, Part B.

ii) Part A is compulsory, which carries 25 marks. In Part A, answer all questions.

iii) In Part B, Answer any one question from each unit. Each question carries 10 marks and may have a, b as sub questions.

PART – A**(25 Marks)**

- 1.a) Define omega notation. [2]
- b) Write an algorithm of binary search. [3]
- c) What is 4-color problem? [2]
- d) Explain about connected components with examples. [3]
- e) What is the important feature of dynamic programming? [2]
- f) Discuss about the reliability design problem. [3]
- g) Give an example of spanning tree. [2]
- h) Briefly explain applications of Greedy method. [3]
- i) Define state space tree. [2]
- j) Explain about Least Cost(LC) Search. [3]

PART – B**(50 Marks)**

- 2.a) Write an algorithm of quick sort.
- b) Explain about big-oh and theta notations. [5+5]

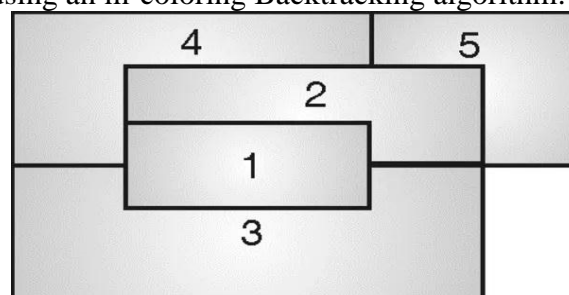
OR

- 3.a) Derive the time complexity of Merge sort.
- b) Distinguish between time complexity and space complexity. [5+5]

4. Consider the sum-of-subset problem, $n = 4$, $\text{Sum} = 13$, and $w_1 = 3$, $w_2 = 4$, $w_3 = 5$ and $w_4 = 6$. Find a solution to the problem using backtracking. Show the state-space tree leading to the solution. Also, number the nodes in the tree in the order of recursion calls. [10]

OR

5. Construct a planar graph for the following map. Explain how to find m-coloring of this planar graph by using an m-coloring Backtracking algorithm. [10]



6. Use the function OBST to compute $w(i,j)$, $r(i,j)$, and $c(i,j)$, $0 \leq i < j \leq 4$, for the identifier set $(a_1, a_2, a_3, a_4) = (\text{cout}, \text{float}, \text{if}, \text{while})$ with $p(1) = 1/20$, $p(2) = 1/5$, $p(3) = 1/10$, $p(4) = 1/20$, $q(0) = 1/5$, $q(1) = 1/10$, $q(2) = 1/5$, $q(3) = 1/20$, and $q(4) = 1/20$. Using the $r(i,j)$'s construct the optimal binary search tree. [10]

OR

7. Define Dynamic programming. Solve the following 0/1 Knapsack Problem using dynamic programming $n=4$, $m=30$, $(w_1, w_2, w_3, w_4) = (10, 15, 6, 9)$ and $(p_1, p_2, p_3, p_4) = (2, 5, 8, 1)$. [10]
8. Show how Prim's algorithm can be implemented using heap. What would be the time complexity of the algorithm? [10]

OR

9. Let $G(V, E)$ be any weighted connected graph.
- a) If C is any cycle of G , then show that the heaviest edge of C cannot belong to a minimum-cost spanning tree of G .
- b) Assume that F is a forest that is a subgraph of G . Show that any F -heavy edge of G cannot belong to a minimum-cost spanning tree of G . [10]

- 10.a) Describe the classes NP-hard and NP-complete in detail.
- b) Write a non-deterministic algorithm of sorting an elements in an array. [5+5]

OR

- 11.a) Briefly explain applications of branch and bound technique.
- b) Write an algorithm LC Branch and Bound. [5+5]

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