

Code No: 181AC

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech I Year I Semester Examinations, September - 2023

BASIC MATHEMATICS

(Bio-Technology)

Time: 3 Hours

Max. Marks: 60

Note: This question paper contains two parts A and B.i) **Part - A** for 10 marks, ii) **Part - B** for 50 marks.

- Part-A is a compulsory question which consists of ten sub-questions from all units carrying equal marks.
- Part-B consists of **ten questions** (numbered from 2 to 11) **carrying 10 marks each**. From each unit, there are two questions and the student should answer one of them. Hence, the student should answer five questions from Part-B.

PART- A**(10 Marks)**

- 1.a) Compute A^2 for the matrix $A = \begin{bmatrix} 2 & -1 & 1 \\ 2 & 3 & 0 \\ 4 & 3 & 2 \end{bmatrix}$. [1]
- b) Find the sum of all the non-real roots of the equation $(x^2 + x - 3)(x^2 + x - 4) = 20$. [1]
- c) Find the real numbers α and β such that $(\alpha + i\beta)(1 + i) = 10i - 4$. [1]
- d) Find the distances of the point $P(-3,5,7)$ from the coordinate axes. [1]
- e) Let x lies in the second quadrant. If $\sin x = \frac{12}{13}$, find the value of $\sec x + \tan x$. [1]
- f) Find the partial fraction decompose of the function $\frac{2x+5}{x^2+5x+6}$. [1]
- g) Evaluate the integral $\int_2^3 3^x dx$. [1]
- h) Find $\lim_{x \rightarrow 0} \frac{\sin x + e^x - 1}{x}$. [1]
- i) Determine the order and degree of the differential equation $y' + 3y = 5e^x$. [1]
- j) In a single throw of two dice, find the probability of getting a total of 10. [1]

PART - B**(50 Marks)**

2. Consider the matrix $A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & -3 \\ 2 & -1 & 3 \end{bmatrix}$. Show that $\det(A) \neq 0$, and hence find A^{-1} . [10]

OR

- 3.a) Let $A = \begin{bmatrix} 3 & 7 - 4i & -2 + 5i \\ 7 + 4i & -2 & 3 + i \\ -2 - 5i & 3 - i & 4 \end{bmatrix}$. Prove or disprove that A is a Hermitian matrix.
- b) Solve the equation $x^4 - 2x^3 - 21x^2 + 22x + 40 = 0$ whose roots are in arithmetic progression. [5+5]

- 4.a) Find the square root of the complex number $-8 - 6i$.
- b) Let $\omega = e^{\frac{2\pi i}{3}}$, $\alpha = \omega + \omega^2 + \omega^4$ and $\beta = \omega^3 + \omega^5 + \omega^6$. Find the quadratic equation whose roots are α and β . [5+5]

OR

- 5.a) Prove or disprove that the points $P(3,3,3)$, $Q(0,6,3)$, $R(1,7,7)$ and $S(4,4,7)$ are the vertices of a square.
- b) Find the equation of the locus of a point which moves such that the ratio of its distance from $(0, 2)$ and $(0, -2)$ is 6. [5+5]
- 6.a) Prove that $\cot x \cot 2x - \cot 2x \cot 3x - \cot 3x \cot x = 1$.
- b) Consider the triangle ΔABC . If the sides of the triangle are $a = 18$, $b = 24$, and $c = 30$ and the $\angle C = 90^\circ$, find $\sin A$, $\sin B$, and $\sin C$. [5+5]

OR

- 7.a) Find the partial fraction decompose of the fraction $\frac{x^2 + 3}{x^3 + x^2 + 3x + 2}$.
- b) Find the partial fraction decompose of the fraction $\frac{x^4 + 2x^3 - 2x^2 + 4x - 1}{x^2 + 2x - 3}$. [5+5]

- 8.a) Find the derivative of the function $\sin\left(\frac{1+x^2}{1-x^2}\right)$.
- b) Discuss the continuity and differentiability of the function $f(x) = \begin{cases} 3x - 2, & 0 < x \leq 1 \\ 2x^2 - x, & 1 < x \leq 2 \\ 5x - 4, & x > 2 \end{cases}$ at $x = 2$. [5+5]

OR

- 9.a) Evaluate the integral $\int \frac{x-1}{\sqrt{x+4}} dx$.
- b) Evaluate the integral $\int_{-\pi}^{\pi} \sin^5 x dx$. [5+5]

- 10.a) Form the differential equation of the family of ellipses having foci on y-axis and centre at origin.
- b) Find the general solution of the differential equation $2ye^{\frac{x}{y}} dx + \left(y - 2xe^{\frac{x}{y}}\right) dy = 0$. [5+5]

OR

- 11.a) If A and B are two events associated with a random experiment such that $P(A) = 0.6$, $P(B) = 0.3$ and $P(A \cap B) = 0.2$, find $P(A \cup B)$.
- b) One number is chosen from numbers 1 to 100. Find the probability that it is divisible by 4 or 6. [5+5]