

Code No: 56017

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech III Year II Semester Examinations, December - 2018

FINITE ELEMENT METHODS

(Common to ME, AE)

Time: 3 hours

Max. Marks: 75

Answer any five questions  
All questions carry equal marks

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- 1.a) Explain your understanding on following terms:  
i) Element, ii) Nodes  
b) Consider a uniform rod subjected to a uniform axial load as illustrated in figure 1. It can be readily shown that the deformation of the bar is governed by the differential equation

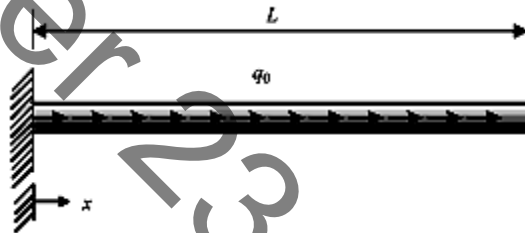


Figure 1

$$AE \frac{d^2 u}{dx^2} + q_0 = 0$$

With the boundary condition,

$$u(0) = 0, \quad \left. \frac{du}{dx} \right|_{x=L} = 0.$$

Let us now find an approximate solution to this problem using the method just discussed. Assume a trial or guess solution. [5+10]

$$u(x) \approx \hat{u}(x) = c_0 + c_1 x + c_2 x^2$$

- 2.a) What do you mean by discretization? Also, differentiate between H-method and P-method.  
b) Rod under distributed and concentrated forces and subjected to forces as shown in figure 2.

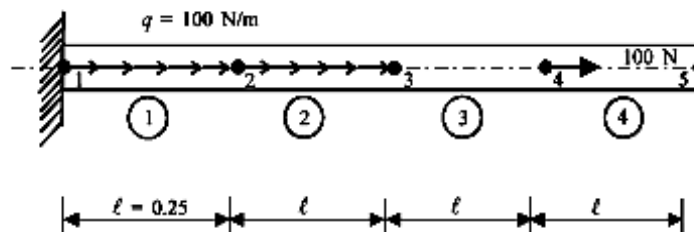


Figure 2

Find nodal displacements.

[5+10]

3. For the truss in figure 3, a horizontal load of  $P = 4000$  lb is applied in the x direction at node 2.
- Write down the element stiffness matrix  $k$  for each element.
  - Assemble the  $K$  matrix.
  - Using the elimination approach, solve for  $Q$ .
  - Evaluate the stress in element 2 and 3.
  - Determine the reaction force at node 2 in the y direction.

[15]

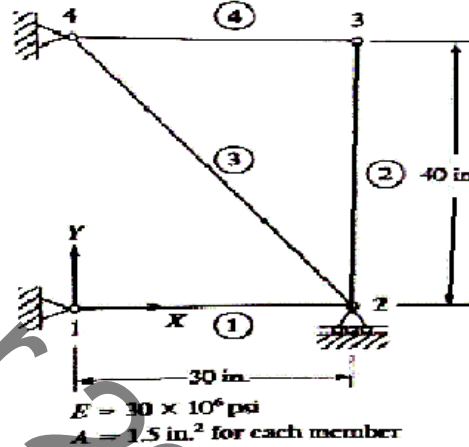


Figure 3

4. The fixed-fixed bar shown in figure 4 has axial forces applied at  $L/3$  and  $2L/3$ . Use the finite element method to compute the axial deflections and support reactions. [15]

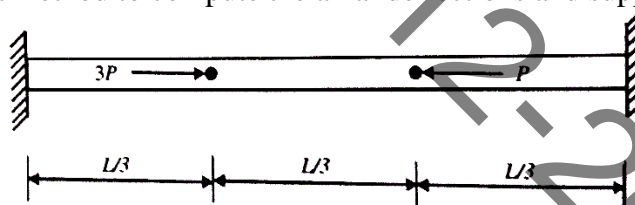


Figure 4

5. Determine the deflection of a thin plate subjected to extensional loads as shown in figure 5. [15]

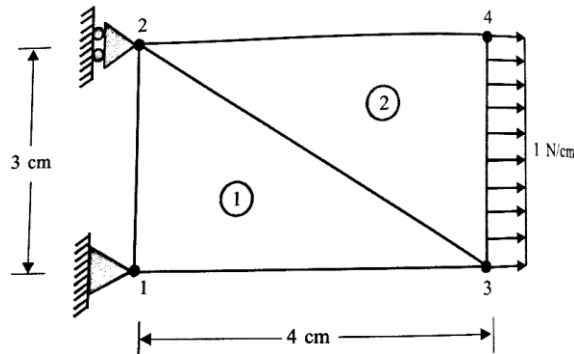


Figure 5

6. Evaluate the shape functions  $N_1$ ,  $N_2$  and  $N_3$  at the interior point  $P$  for the triangular element shown in figure 6. [15]

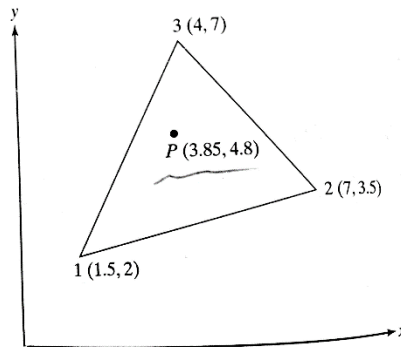


Figure 6

7. The plane wall shown in figure 7. Is 1 m thick. The left surface of wall is maintained at a constant temperature of  $500^\circ\text{C}$ , and the right surface is insulated. The thermal conductivity  $k=25\text{W/m}^\circ\text{C}$ , and there is uniform heat generation inside the wall of  $Q = 400\text{ W/m}^3$ . Determine the temperature distribution through the wall thickness using linear elements. [15]

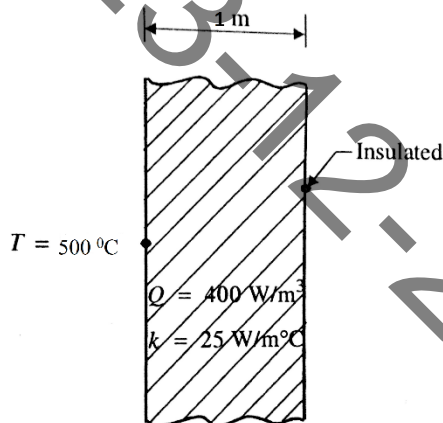


Figure 7

- 8.a) Difference between forward and inverse iterations.  
 b) Consider the underdamped, 2 - d.o.f. system shown in figure 8. Find the response of the system when the first mass alone is given an initial displacement of unity and released from rest. [5+10]

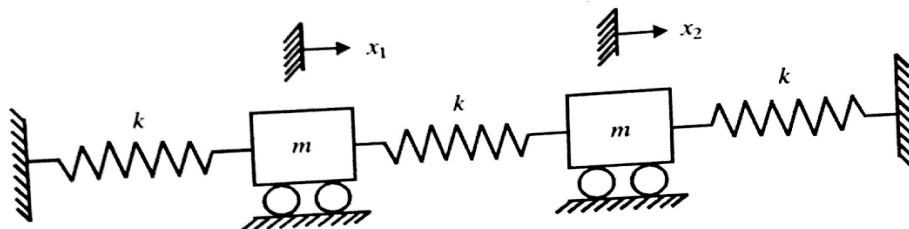


Figure 8