

Code No: 56083

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech III Year II Semester Examinations, February/March - 2022

NUMERICAL METHODS

(Automobile Engineering)

Time: 3 hours

Max. Marks: 75

Answer any five questions
All questions carry equal marks

- 1.a) Find a real root of the equation of $x^3 + x^2 - 1 = 0$ by iteration method.
b) Find a root of $x \tan x + 1 = 0$ by Newton Raphson method. [8+7]

2. Solve the system of equations using Gauss Seidal method:
 $x + 5y + 2z = 7$
 $7x - y + z = 2$
 $x + 2y + 5z = 9$ [15]

- 3.a) Find $y(32)$ if $y(10)=35.3$, $y(15) = 32$, $y(20) = 29.2$, $y(25) = 26.1$, $y(30) = 23.2$, $y(35) = 20.5$ using Newton's forward formula.
b) Find $y(1.6)$ if $y(1.2) = 1.36$, $y(2.0) = 0.58$ and $y(2.5) = 0.34$, $y(3.0) = 0.20$ using Lagranges formula. [7+8]

4. Fit a parabola $y = a + bx + cx^2$ to the following data: [15]

x	1	2	3	4	5	6	7
y	2.3	5.2	9.7	16.5	29.4	35.5	54.4

5. Find $\int_0^1 \frac{dx}{1+x^2}$ using 10 intervals using a) simpson $\frac{1}{3}$ rd's rule b) simpson $\frac{3}{8}$ th's rule. [15]

6. Find $y(0.1)$ and $y(0.2)$ using Taylor's series method given that $y' = y^2 + x$ and $y(0) = 1$, $h = 0.1$. [15]

7. Find the values of $y(0.25)$, $y(0.5)$ and $y(0.75)$ by finite difference method, given that $y'' - 4y = 8$, $y(0) = 0$, $y(1) = 0$, Compare the results with the exact values and find the percentage error. [15]

8. Find the numerical solution of $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ for $h = 0.2$, $0 \leq x \leq 1$, $t \geq 0$, with the boundary conditions. [15]

$$u(0, t) = u(1, t) = 0, \quad u(x, 0) = \begin{cases} 2x, & 0 \leq x \leq \frac{1}{2} \\ 2(1-x), & \frac{1}{2} \leq x \leq 1 \end{cases}$$

at $i = 1, 2, 3, 4, 5$ and
 $j = 1, 2, 3, 4, 5$

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