

Code No: 155SE

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech III Year I Semester Examinations, February - 2022

ELECTROMAGNETIC FIELDS AND WAVES

(Electronics and Communication Engineering)

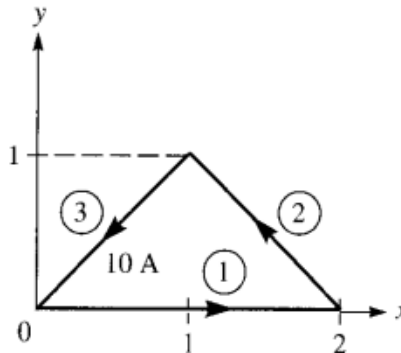
Time: 3 hours

Max. Marks: 75

Answer any five questions
All questions carry equal marks

- 1.a) In a certain region, the electric field is given by

$$D = 2\rho(z + 1)\cos\phi a_\rho - \rho(z + 1)\sin\phi a_\phi + \rho^2 \cos\phi a_z \mu C/m^2$$
 i) Find the charge density.
 ii) Calculate the total charge enclosed by the volume $0 < \rho < 2, 0 < \phi < \frac{\pi}{2}, 0 < z < 4$.
- b) In free space $D = 2y^2 a_x + 4xy a_y - a_z mC/m^2$. Find the total charge stored in the region $1 < x < 2, 1 < y < 2, -1 < z < 4$. [8+7]
- 2.a) State Gauss's law. Deduce Coulomb's law from Gauss's law thereby affirming that Gauss's law is an alternative statement of Coulomb's law and that Coulomb's law is implicit in Maxwell's equation $\nabla \cdot D = \rho_v$.
- b) A cylindrical capacitor has radii $a=1\text{cm}$ and $b=2.5\text{cm}$. If the space between the plates is filled with an inhomogeneous dielectric with $\epsilon_r = (10 + \rho)/\rho$, where ρ is in centimeters, find the capacitance per meter of the capacitor? [10+5]
- 3.a) Find H at (0,0,5) due to side 3 of triangular loop shown in figure below.



- b) Prove that the line integral of the tangential component of H around a closed path is the same as the net current enclosed by the path. [8+7]
- 4.a) For a current distribution in free space

$$A = (2x^2y + yz)a_x + (xy^2 - xz^3)a_y - (6xyz - 2x^2y^2)a_z \text{ Wb/m}$$
 i) Calculate B.
 ii) Calculate H.
 iii) Find the magnetic flux through a loop described by $x=1, 0 < y, z < 2$.
 iv) Show that $\nabla \cdot B = 0$
 v) Show that $\nabla \cdot A = 0$
- b) State and prove Faraday's Law. [10+5]

5.a) Check whether the following field is satisfy Maxwell's equations:

$$\left(3\rho^2 \cot\theta a_\rho + \frac{\cos\theta}{\rho} a_\theta\right) \sin\omega t$$

Assume that the fields exist in charge free regions.

- b) Derive the boundary conditions for electric fields between dielectric to conductor surface. [9+6]
- 6.a) A plane wave propagating through a medium with $\epsilon_r = 8, \mu_r = 2$ has $E = 0.5e^{-z/3} \sin(10^8 t - \beta z) a_x V/m$. Determine β , loss tangent, wave impedance, wave velocity, and H field.
- b) In free space $H = 0.2 \cos(\omega t - \beta x) a_z A/m$. Find the total power passing through a circular disc of radius 5 cm on plane $x=1$. [10+5]
- 7.a) Derive the equation for reflection and transmission coefficients for the plane wave with oblique incidence with E perpendicular to the plane of incidence.
- b) What are the advantages and limitations of microstrip lines? [10+5]
- 8.a) Derive the equation for cutoff frequency, wave impedance for rectangular waveguide in TE mode starting from Maxwell's equations.
- b) A standard air-filled rectangular waveguide with dimensions $a=8.636\text{cm}$, $b=4.318\text{ cm}$ is fed by a 4-GHz carrier from a coaxial cable. Determine if a TE_{10} mode will be propagated. If so, calculate the phase velocity and group velocity. [8+7]

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